Deep Feature Mining via Attention-based BiLSTM-GCN for Human Motor Imagery Recognition

Shuyue Jia, Jan. 15th, 2023

Tasks

✓ Electroencephalogram (EEG) Tasks Classification



Control a wheelchair via EEG



Interpret Functional Networks and better understand human brain

Image Credit: in the public domain.

EEG Research Novelty

- ✓ [Motivation] Graph Modeling for EEG Electrodes System
- ✓ [Method] Graph Representation Learning of EEG Signals
- ✓ [Motivation] Spatial-Temporal Analysis of EEG Signals
- ✓ [Method] Deep Feature Mining of EEG Signals



International 10-10 EEG System





Attention-based Bidirectional Long Short-term Memory (Bi-LSTM)





GCNs-Net: A Graph Convolutional Neural Network Approach for Decoding Time-Resolved EEG Motor Imagery Signals

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EEG Deep Learning Library: https://github.com/SuperBruceJia/EEG-DL

Background

- **BCI**: establish connections between the brain and machines
 - (1) Acquire and analyze brain signals while conducting actual or imagery tasks
 - (2) Control machines
- **Significance**: help the disabled and understand the human brain
- **Types of BCI:**
 - ► Electroencephalography (EEG)
 - Magnetoencephalography (MEG)
 - ► Functional Magnetic Resonance Imaging (fMRI)
 - ▶ Invasive BCI Technologies (*e.g.*, Neuralink)
- **Reasons for using EEG for this project:**
 - Non-Invasiveness
 - ▶ High Temporal Resolution
 - Portability

- A potential market
- Inexpensive Equipment



- **Specific Task**: EEG Motor Imagery (*e.g.*, control a wheelchair via imagery-based EEG signals)
- **Our Research**: develop EEG-based BCI technologies to improve current stroke rehabilitation strategies

Image Credit: in the public domain.

Key Points in dealing with EEG time series

► Individual Variability → Lower Classification Accuracy



Motivation

Convolutional Neural Networks:



- Modeling: Euclidean-Structured Data (e.g., Image, Speech, Natural Language)
- Neuroscience research has increasingly emphasized Brain Network Dynamics
 - Model **Functional Topological Connectivity** of EEG Electrodes → **Graph** (Non-Euclidean Structure)







Image Credit: The PhysioNet Dataset and the Functional Network Image is in the public domain.

Can we directly apply convolutions on graphs?

Traditional CNN cannot directly process graph signals

- **Graph is irregular** (*i.e.*, unordered and vary in size)
- Convolution cannot keep Translation Invariance on non-Euclidean signals
- Graph Convolutional Neural Networks (GCN)
 - Directly process non-Euclidean graph-structured signals
 - Consider relational properties (*e.g.*, correlations) between nodes
 - \rightarrow Model Functional Topological Relationships among EEG electrodes
 - → Analyze and interpret **Brain Network Dynamics**



Benchmark Dataset

- The PhysioNet Dataset (EEG Motor Movement/Imagery Dataset)
- International 10-10 EEG System \rightarrow 64 electrodes

(excluding electrodes Nz, F9, F10, FT9, FT10, A1, A2, TP9, TP10, P9, and P10)



- **109 subjects** (the largest number of participants in the field of EEG Motor Imagery)
- Task: 4-class EEG Motor Imagery Classification
 - Imagining (Task 1) left fist, (Task 2) right fist, (Task 3) both fists, (Task 4) both feet
- Each subject \rightarrow 3 runs, 7 trials, 4 classes \rightarrow 84 trials in total
- Each trial \rightarrow 4 seconds experimental duration, 160 Hz Sampling Rate \rightarrow 640 Time Points
- We apply the **Time-resolved Sampling Method**
 - \checkmark Total samples per subject: 3 runs \times 7 trials \times 4 classes \times 4 seconds \times 160 Hz = 53,760 samples
 - Experimental Setting: 90% as the training set and the left 10% as the test set

Image Credit: The PhysioNet Dataset and the middle image is in the public domain.

Preliminary: Graph Representation

Definition: An Undirected and Weighted Graph with N nodes: $\mathbf{G} = \{\mathbf{V}, \mathbf{E}, \mathbf{A}\}$

- V: nodes (vertices), $|\mathbf{V}| = N$
- E: edges (links) that connect nodes
- A: weights (correlations) between nodes

Nodes Correlations: Pearson Matrix $\mathbf{P} \in \mathbb{R}^{N \times N}$ (denotes as PCC matrix)

- Measure the linear correlations between node \mathbf{x} and node \mathbf{y}
- $-\mu$ is the mean, σ is the standard deviation, and $P_{x,y}$ is the Pearson Correlation Coefficient between node x and node y

$$P_{x,y} = \frac{\mathrm{E}((\mathbf{x} - \mu_x)(\mathbf{y} - \mu_y))}{\sigma_x \sigma_y}$$

- Absolute Pearson Matrix: $|\mathbf{P}| \in \mathbb{R}^{N \times N}$ and $|P_{ij}| \in [0, 1] \rightarrow \text{Note}$: In this work, we only consider scale.

Graph Weights: Adjacency Matrix $\mathbf{A} = |\mathbf{P}| - \mathbf{I} \in \mathbb{R}^{N \times N}$, where **I** is an Identity Matrix **Graph Degrees**: Degree Matrix $\mathbf{D} \in \mathbb{R}^{N \times N}$

$$D_{ii} = \sum_{j=1}^{N} A_{ij}$$

Graph Representation: Combinatorial Laplacian $\mathbf{L} \in \mathbb{R}^{N \times N}$

$$\mathbf{L} = \mathbf{D} - \mathbf{A}$$

Normalized:

$$\mathbf{L} = \mathbf{I} - \mathbf{D}^{-\frac{1}{2}} \mathbf{A} \mathbf{D}^{\frac{1}{2}}$$



Preliminary:

Spectral Theorem for Graph Laplacian L

 $\mathbf{L} = \mathbf{U} \mathbf{\Lambda} \mathbf{U}^{\mathrm{T}}$ $\mathbf{L} \mathbf{U} = \mathbf{\Lambda} \mathbf{U}$

– U: Fourier basis \rightarrow real and orthonormal <u>eigenvectors</u> of L

- Λ : Fourier modes \rightarrow the diagonal is the **ordered** and **real nonnegative** <u>eigenvalues</u> of L

Graph Fourier Transforms of Signal f

can be seen as the $e^{-j\omega t}$ in Fourier Transforms

$$F[f(\boldsymbol{\lambda})] = \hat{f}(\boldsymbol{\lambda}) = \sum_{i=1}^{n} f(i) \times U(i)$$

$$\hat{f}(\boldsymbol{\lambda}) = \mathbf{U}^{\mathrm{T}} f \Leftrightarrow f = \mathbf{U} \hat{f}(\boldsymbol{\lambda})$$

 $\hat{f}(\boldsymbol{\lambda})$ is the projection value of the Fourier basis **U**

Preliminary: Graph Convolution via Graph Fourier Transform

Notation:

Signal f

Signal *h*

F: Fourier Transforms

F⁻¹: Inverse Fourier Transforms

 $\hat{f}(w)$: F(f)

 $\hat{h}(w)$: F(h)

Note: Fourier Transforms of **Convolution in the spatial domain** \Leftrightarrow Point-wise Multiplication of two Fourier transformed signals $F((f * h)_{\mathbf{G}}) = \hat{f}(w) \times \hat{h}(w)$ Convolution $(f * h)_{\mathbf{G}} = \mathbf{F}^{-1}(\hat{f}(w) \times \hat{h}(w))$ Hadamard Product $\hat{f}(\lambda) = \mathbf{U}^{\mathrm{T}} f$ (Element-wise Multiplication) $(f * h)_{\mathbf{G}} = \mathbf{F}^{-1} \left((\mathbf{U}^{\mathrm{T}} f) \odot (\mathbf{U}^{\mathrm{T}} h) \right)$ $f = \mathbf{U}\hat{f}(\lambda)$ $(f * h)_{\mathbf{G}} = \mathbf{U} \left((\mathbf{U}^{\mathrm{T}} f) \odot (\mathbf{U}^{\mathrm{T}} h) \right)$ $[\mathbf{n} \times \mathbf{n}]$ $[\mathbf{n} \times \mathbf{n}]$ $[\mathbf{n} \times \mathbf{n}]$ $(f * h)_{\mathbf{G}} = \mathbf{U} \operatorname{diag}[\hat{h}(\lambda_{1}), \hat{h}(\lambda_{2}), ..., \hat{h}(\lambda_{n})]\mathbf{U}^{\mathrm{T}} f$ $[\mathbf{n} \times \mathbf{d}]$

Source: https://en.wikipedia.org/wiki/Convolution_theorem

Graph Convolution



Credit: Defferrard et al., Convolutional Neural Networks on Graphs with Fast Localized Spectral Filtering, In NeurIPS 2016.



GCN Key Idea: Use "edge information" to aggregate "node information" to generate a new "node representation"



- Pros:
- 1. No need for Spectral Decomposition of L
- 2. Less number of parameters (decrease model complexity) $\rightarrow K \ll N$
- Cons: Need to compute \mathbf{L}^k

Pooling on Graphs (Graph Coarsening)

- Traditional CNN doesn't need to consider neighbors after convolutions
 - [Euclidean Structure] The output Feature Maps are "regular"
 - The neighbor is "meaningful"
- GCNs need to consider neighbors after convolutions



- [Non-Euclidean Structure] The output graphs' nodes are not arranged in any meaningful way
- Use Graclus Multilevel Clustering Algorithm to find "meaningful" neighbors
- Minimize the *Local Normalized Cut* (a cluster grouping method)

$$-W_{ij}(\frac{1}{d_i} + \frac{1}{d_j})$$

- i and j denote node i and node j
- W_{ij} is the **learned weight** between node i and node j





Correlation among EEG electrodes Two Subjects: Subject 10 and 5



Fig. 6. PCC matrix, absolute PCC matrix, adjacency matrix, and graph Laplacian for Subjects 10 and 5 from the PhysioNet dataset. (a) PCC matrix for Subject 10. (b) Absolute PCC matrix for Subject 10. (c) Adjacency matrix for Subject 10. (d) Graph Laplacian for Subject 10. (e) PCC matrix for Subject 5. (f) Absolute PCC matrix for Subject 5. (h) Graph Laplacian for Subject 5.

Correlation among EEG electrodes 20 Subjects and 100 Subjects



Fig. 2. PCC matrix, absolute PCC matrix, adjacency matrix, and graph Laplacian for 20 and 100 subjects, respectively, from the PhysioNet dataset. (a) PCC matrix for 20 subjects. (b) Absolute PCC matrix for 20 subjects. (c) Adjacency matrix for 20 subjects. (d) Graph Laplacian for 20 subjects. (e) PCC matrix for 100 subjects. (f) Absolute PCC matrix for 100 subjects. (g) Adjacency matrix for 100 subjects. (h) Graph Laplacian for 100 subjects.

Increasing the number of subjects alleviates individual variability

Model Design for 64-electrode EEG System

TABLE I

Layer	Туре	Maps	Size	Edges	Polynomial Order	Pooling Size	Activation	Weights	Bias
Softmax	Fully-connected	_	О	_	_	_	Softmax	$\frac{N}{64} \times \frac{N}{64} \times F_6 \times O$	0
Flatten	Flatten	_	$rac{N}{64} imes rac{N}{64} imes F_6$		_	_	_	<u> </u>	_
P6	Max-pooling	F_6	$\frac{\mathrm{N}}{32}$	$\sum_{i=1}^{\frac{N}{32}-1} i$	_	2	—	_	—
C6	Convolution	F_6	$\frac{N}{32}$	$\sum_{i=1}^{rac{\mathrm{N}}{32}-1} i$	Κ	_	Softplus	$\mathrm{F}_5 \times \mathrm{F}_6 \times \mathrm{K}$	$rac{N}{32} imes F_6$
P5	Max-pooling	F_5	$\frac{N}{16}$	$\sum_{i=1}^{\frac{1}{16}-1} i$	_	2	—	_	—
C5	Convolution	F_5	$\frac{N}{16}$	$\sum_{i=1}^{\frac{N}{16}-1} i$	Κ	_	Softplus	$F_4 \times F_5 \times K$	$\frac{N}{16} \times F_5$
P4	Max-pooling	F_4	$\frac{N}{8}$	$\sum_{i=1}^{\frac{N}{8}-1} i$	_	2	_	_	_
C4	Convolution	F_4	$\frac{N}{8}$	$\sum_{i=1}^{\frac{N}{8}-1} i$	Κ	_	Softplus	$\mathrm{F}_3 \times \mathrm{F}_4 \times \mathrm{K}$	$\frac{N}{8} \times F_4$
P3	Max-pooling	F_3	$\frac{N}{4}$	$\sum_{i=1}^{\frac{N}{4}-1} i$	_	2	_	_	_
C3	Convolution	F_3	$\frac{N}{4}$	$\sum_{i=1}^{\frac{N}{4}-1} i$	Κ	_	Softplus	$\mathrm{F}_2 \times \mathrm{F}_3 \times \mathrm{K}$	$\frac{N}{4} \times F_3$
P2	Max-pooling	F_2	$\frac{N}{2}$	$\sum_{i=1}^{\frac{N}{2}-1} i$	_	2	_	_	_
C2	Convolution	F_2	$\frac{N}{2}$	$\sum_{i=1}^{\frac{N}{2}-1} i$	Κ	_	Softplus	$F_1 \times F_2 \times K$	$\frac{N}{2} \times F_2$
P1	Max-pooling	\mathbf{F}_{1}	Ñ	$\sum_{i=1}^{N-1} i$	_	2	_	—	
C1	Convolution	F_1	Ν	$\sum_{i=1}^{N-1} i$	Κ	_	Softplus	$1\times F_1\times K$	$\mathrm{N}\times\mathrm{F}_1$
Input	Input	1	Ν	$\sum_{i=1}^{N-1} i$	—	—	—	—	_

IMPLEMENTATION DETAILS OF THE PROPOSED GCNS-NET ON THE PHYSIONET DATASET

Model Optimization

- Ablation Study: Optimal Model Structure (64-electrode EEG System)
 - C6-P6-K2 with [16, 32, 64, 128, 256, 512] filters
- Gradient Iterative Solver: Adam Optimizer with Stochastic Gradient Descent (SGD) algorithm
 - Learning Rate: 0.01
 - Batch Size: 1,024

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• Activation Function: Softplus (Smooth Rectified Linear Unit)

 $F(\mathbf{x}) = \log(1 + e^{\mathbf{x}})$

• **Model Output**: Softmax: y are labels, \hat{y} are the final output tasks

$$\widehat{y}_i = \operatorname{argmax}\left(\frac{\mathrm{e}^{y_i}}{\sum_{i=1}^4 \mathrm{e}^{y_i}}\right)$$

Loss Function: Cross-entropy Loss with L2 regularization

$$\text{Loss} = -\sum_{i=1}^{4} y_i \log(\widehat{y_i}) + \lambda \left(\sum_{j=1}^{n} w_j^2 + b_j^2\right)$$

 $\lambda = 1 \times 10^{-6}$ is the coefficient of the L2 regularization.

Ablation Study



Fig. 3. Accuracy of some selected models regarding different polynomial approximation order. The models are selected from Table II. (a) Accuracy of the model C1-P1 (model 1). (b) Accuracy of the model C2-P2 (model 3). (c) Accuracy of the model C3-P3 (model 6). (d) Accuracy of the model C4-P4 (model 10). (e) Accuracy of the model C5-P5 (model 14). (f) Accuracy of the model C6-P3 (model 16). (g) Accuracy of the model C6-P5 (model 19). (h) Accuracy of the model C6-P6 (model 20).

Experimental Results Groupwise Prediction and Subject-specific Adaptation

TABLE IV

PERFORMANCE COMPARISONS ON THE PHYSIONET DATASET

Related Work	Max. Accuracy	Avg. Accuracy	<i>p</i> -value	Level	Approach	Num. of Subjects
Dose et al. (2018) [22]	80.38%	58.58% 68.51%		Group Subject	CNNs	105 1
Ma et al. (2018) [60]	82.65%	68.20%	_	Group	RNNs	12
Hou et al. (2020) [20]	94.50% 96.00%	_	- > 0.05	Group Subject	ESI-CNNs	10 1
Hou et al. (2022) [34]	94.64% 98.81%	 95.48%	- > 0.05	Group Subject	BiLSTM-GCN	20 1
Jia et al. (2022) [40]	94.16% 98.08%	93.78% 94.18%	- > 0.05	Group Subject	Graph ResNet	20 1
Author	89.39% 88.14% 98.72%	88.57% 93.06%	_	Group Subject	GCNs-Net	20 100 1

Note: p-value $< 0.05 \rightarrow$ Statistically Significant Difference

Takeaways and Future Work

✓ Graph Representation

Graph Representation Learning to deeply extract Network Patterns of Brain Dynamics for EEG classification.

✓ Model Converge

Converge for both <u>Personalized and Groupwise Predictions</u>, indicating that the GCNs-Net is able to build a generalized representation of EEG time-series against both <u>Personalized and Groupwise Variations</u>.

✓ Future Work

Model EEG signals as Dynamic Graphs and process them via Dynamic Graph Representation Learning.

Deep Feature Mining via Attention-based BiLSTM-GCN for Human Motor Imagery Recognition

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EEG Deep Learning Library: https://github.com/SuperBruceJia/EEG-DL

One Problem of the GCNs-Net



 $\checkmark \quad \text{GCNs-Net is based on Time-resolved Signal} \rightarrow \text{doesn't consider Temporal Information}$

Motivation:

- [Spatial-Temporal Analysis] Consider Temporal and Spatial Information from EEG signals
- ✓ [Responsive] Maintain High Responding Time

Image Credit: The PhysioNet Dataset.

64-channel Raw EEG Signals Acquisition



- ✓ 4-s Signals (experimental duration): **0.4-s segments** over time
- ✓ Each Segment: **64 channels** × **64 time steps**
- Pre-processed Data: Temporal Information + Spatial Information

Temporal Information Extraction



Recurrent Neural Network (RNN)



Long-term State

Short-term

State

- ✓ Designed for order-mattered sequential data, *e.g.*, time series
- ✓ The learned features at *time step t* are affected by \mathbf{x}_t and $\mathbf{x}_{t-1} \rightarrow \textbf{continuly learn}$ from time series
- ✓ LSTM: better capture **long-range sequence dependencies**
- ✓ Gated Recurrent Units (GRU): lightweight architecture with comparable performance

Image Credit: LeCun et al., Deep Learning, In Nature.

Long Short-term Memory (LSTM)



✓ Capture Long-range Dependencies by the long-term state path $c_{t-1} \rightarrow c_t$

- ✓ **Input Gate**: store \mathbf{x}_t and control \mathbf{c}_t 's input
- **Forget Gate**: control **c**_{t-1}
- ✓ **Output Gate**: control c_t 's output
 - \rightarrow short-term state h_t (Cell's Output)
- ✓ More parameters to store information
- ✓ Bidirectional:
 - (1) $\mathbf{x}_1 \rightarrow \mathbf{x}_t$ (2) $\mathbf{x}_t \rightarrow \mathbf{x}_1$



Attention Mechanism

Signals or Outputs

 \checkmark

Equally treated/contributed

VS.

<u>Differently</u> treated/contributed <u>with preference/importance</u>

FC Layer
$$\mathbf{U}_{t} = \tanh(\mathbf{W}_{w}\mathbf{y}_{t} + \mathbf{b}_{w})$$

Attentional Weights

> Weighted Sum

$$\widehat{\mathbf{U}}_t = \sum_t \boldsymbol{\alpha}_t \mathbf{y}_t$$

 $\boldsymbol{\alpha}_{t} = \frac{\exp(\mathbf{U}_{t}^{\mathrm{T}}\mathbf{W}_{U})}{\sum_{t}\exp(\mathbf{U}_{t}^{\mathrm{T}}\mathbf{W}_{U})}$

Image Credit: Prof. Bolei Zhou.

Attention-based Bidirectional Long Short-term Memory (Bi-LSTM)



Model Design Ablation Study



Fig. 3: Models and Hyperparameters Comparison w.r.t. the RNN-based Methods for Feature Extraction

Topological Structure of Features



✓ Deep Feature Mining → Intra-feature Relationship → Intra-feature Modeling



Topological Structure of Features



0.9

0.7

0.5

0.2

30

25

20

15

Fig. 4: The Pearson, Absolute Pearson, Adjacency, and Laplacian Matrices for Subject Nine.

Experimental Results - Groupwise Prediction



Fig. 5: Box plot and confusion matrix for 10-fold cross validation.

Note:

- (1) Box Plot (Maximum Score, Upper Quartile, Median, Lower Quartile, and Minimum Score)
- (2) Confusion Matrix: TP, TN, FP, and FN

Experimental Results - Subject-Specific Adaptation

No. of Subject	GAA	Карра	Precision	Recall	F1 Score
1	94.05%	92.06%	94.20%	94.32%	94.16%
2	96.43%	95.19%	96.06%	96.06%	96.06%
3	97.62%	96.79%	97.33%	97.08%	97.18%
4	90.48%	87.34%	91.30%	91.11%	90.42%
5	95.24%	93.61%	95.96%	95.06%	95.38%
6	94.05%	92.02%	93.40%	94.96%	93.66%
7	98.81%	98.40%	98.81%	99.07%	98.92%
8	95.24%	93.60%	95.39%	95.04%	95.19%
9	98.81%	98.39%	99.11%	98.68%	98.87%
10	94.05%	91.98%	93.39%	94.70%	93.61%
Average	95.48%	93.94%	95.50%	95.61%	95.35%

TABLE II: Subject-level Evaluation

TABLE III: Current studies comparison on subject-level prediction

Related Work	Max. GAA	Approach	Database
Ortiz-Echeverri et al. (2019)	94.66%	Sorted-fast ICA-CWT + CNNs	
Sadiq et al. (2019)	95.20%	EWT + LS-SVM	BCI Competition IV-a Dataset
Taran <i>et al.</i> (2018)	96.89%	TQWT + LS-SVM	
Zhang <i>et al.</i> (2019)	83.00%	CNNs-LSTM	
Ji et al. (2019)	95.10%	SVM	BCI Competition IV-2a Dataset
Amin et al. (2019)	95.40%	MCNNs	
Dose et al. (2018)	68.51%	CNNs	
Hou et al. (2019)	96.00%	ESI + CNNs	Physionet Database
This work	98.81%	Attention-based BiLSTM-GCN	-

Takeaways and Future Work

✓ Spatial-Temporal Analysis

(1) Converge to both **Subject-level and Groupwise Predictions** and handle **Individual Variability**.

(2) The 0.4-s sample size <u>Time-Resolved Solution</u> toward fast response.

✓ Deep Feature Mining

- (1) ↑ Highest Accuracy
- (2) Advance <u>Clinical Translation</u> of EEG-based BCI technology to meet diverse demands, such as those of paralyzed patients.

✓ Future Work

Long-range Dependencies among intra-subject or inter-subject EEG signals can be modeled via Non-local Modeling, Self-attention Mechanism, Transformer, and AI foundation Models.

Thank you!

Any question?

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